FAA NEXTOR NAS Performance Workshop, Asilomar, 4/14/2009

#### Analyzing Aircraft Taxi Times at Airports: Comparison and Decomposition

Yu Zhang, Arjun Chauhan University of South Florida

## BTS Report (1)



## BTS Report (2)



## Roadmap

- Review and compare taxiing time models
  - Existing model
  - Alternative model
- Decompose taxiing time
  - Taxi time according to scheduling
  - Excess taxi time
- Work in-progress
  - Integrated Model for Departure Sequence and Gate Push-back Times
  - Impact of Airport Delay on National System

#### Causal Factors Affecting Taxi Times

- Arrival and departure demands
- Arrival and departure queue lengths
- Runway configuration
- Airline/terminal
- Weather and upstream and downstream restrictions
- Other factors

## **Exiting Model**

- Group: Origin-Destination, Carrier, Season
- Excluding the upper 25% taxiing time in estimation
- Departure queue length: the number of aircraft ahead of the flight at the queue entry time (gate out time)
- Arrival queue length: the number of aircraft ahead of the flight at the queue entry time (wheel-on time).



## **Exiting Model**

- Group: Origin-Destination, Carrier, Season
- Excluding the upper 25% taxiing time in estimation
- Departure queue length: the number of aircraft ahead of the flight at the queue entry time (gate out time)
- Arrival queue length: the number of aircraft ahead of the flight at the queue entry time (wheel-on time).

Regression model:

$$y_o = a \cdot x_o + b \cdot x_i + c$$
$$y_i = a' \cdot x_o + b' \cdot x_i + c'$$

Unimpeded taxi time:

$$y_o^* = a \cdot 1 + b \cdot 0 + c$$
$$y_i^* = a' \cdot 0 + b' \cdot 1 + c'$$

#### Aircraft Over Passing<sup>1</sup>



## **Alternative Model**

- Group: Origin-Destination, Carrier, Season
- Excluding the upper 25% taxiing time in estimation
- Departure queue length: <u>the</u> <u>number of takeoffs that took</u> <u>place ahead of the reference</u> <u>aircraft during its taxi out.</u>
- Arrival queue length: <u>the</u> <u>number of aircraft that gated</u> <u>in ahead of the reference</u> <u>aircraft during its taxi in.</u>



## **Alternative Model**

- Group: Origin-Destination, Carrier, Season
- Excluding the upper 25% taxiing time in estimation
- Departure queue length: <u>the</u> <u>number of takeoffs that took</u> <u>place ahead of the reference</u> <u>aircraft during its taxi out.</u>
- Arrival queue length: <u>the</u> <u>number of aircraft that gated</u> <u>in ahead of the reference</u> <u>aircraft during its taxi in.</u>

Regression model:

$$T_o = \alpha \cdot q_o + \beta \cdot q_i + \gamma$$
$$T_i = \alpha' \cdot q_o + \beta' \cdot q_i + \gamma'$$

Unimpeded taxi time:

$$T_o^* = \alpha \cdot 1 + \beta \cdot 0 + \gamma$$
$$T_i^* = \alpha' \cdot 0 + \beta' \cdot 1 + \gamma'$$

## Comparison of two Models

<b>R-square Statistics</b>	Existing Model	Alternative Model
Mean	0.32	0.62
Standard Error	0.01	0.01
Median	0.32	0.64
Mode	0.36	0.68
Standard Deviation	0.11	0.12
Sample Variance	0.01	0.02
Kurtosis	0.83	4.41
Skewness	0.33	-1.53
Range	0.79	0.87
Minimum	0.00	0.01
Maximum	0.79	0.88
Group	439	439 11

## Decompose Taxi time

- Taxi time with scheduled departure and arrival demands assuming regular operational environment
- Taxi time affected by other factors

#### Iterative Algorithm for Decomposing Taxi Times

1. Initialization :

$$x_o^{(0)} \leftarrow 0 \text{ and } x_i^{(0)} \leftarrow 0$$

iteration count  $n \leftarrow 1$ 

convergence parameter  $\varepsilon = 0.005$ 

2. Given estimated coefficients from regression model, calculate

$$t_{o}^{(n)} = a \cdot x_{o}^{(n-1)} + b \cdot x_{i}^{(n-1)} + c$$

 $t_i^{(n)} = a' \cdot x_o^{(n-1)} + b' \cdot x_i^{(n-1)} + c'$ 

3. Given scheduled departure time *d* and scheduled gate in time  $g_i$ calculate gate out time  $g_o^{(n)} = d - t_o^{(n)}$ and arrival time  $a^{(n)} = g_i - t_i^{(n)}$  4. Calculate departure and arrival queue lengths  $x_o^{(n)}$  and  $x_i^{(n)}$ , assuming no overpassing 5. Given estimated coefficients from regression model, calculate  $t_{a}^{(n+1)} = a \cdot x_{a}^{(n)} + b \cdot x_{i}^{(n)} + c$  $t_i^{(n+1)} = a' \cdot x_o^{(n)} + b' \cdot x_i^{(n)} + c'$ 6. Convergence test : If  $\sum_{s} \left( t_i^{(n+1)} - t_i^{(n)} \right) / F_a < \varepsilon$ and  $\sum_{i} \left( t_o^{(n+1)} - t_o^{(n)} \right) / F_d < \varepsilon$ stop else n  $\leftarrow$  n + 1 and go to step 3 12

## Numerical Example (Taxi-in)

	Unimpeded_TI	Nominal_TI	Actual_TI
Mean	5.39	6.74	7.50
Standard Error	0.04	0.05	0.21
Median	5.30	6.18	7.00
Mode	5.30	3.84	7.00
Standard Deviation	0.92	1.05	4.59
Sample Variance	0.84	1.10	21.08
Kurtosis	1.20	-0.87	25.82
Skewness	0.89	-0.13	3.84
Range	4.50	5.42	52.00
Minimum	4.00	3.84	1.00
Maximum	8.50	9.26	53.00
Sum	2467.00	2752.56	3433.00
Count	458	458	458

#### Taxi-in (Mean by Hour)

Taxi-in Times



#### Taxi-in (Mean and Range by Hour)

#### Taxi-in Times



## Numerical Example (Taxi-out)

	Unimpeded_TO	Nominal_TO	Actual_TO
Mean	12.60	20.29	37.56
Standard Error	0.07	0.12	1.56
Median	12.4	19.84	25
Mode	12.4	15.14	23
Standard Deviation	1.47	2.51	33.63
Sample Variance	2.16	6.29	1130.99
Kurtosis	-0.91	-0.13	7.52
Skewness	0.40	0.06	2.64
Range	5.1	13.55	195
Minimum	10.1	14.24	9
Maximum	15.2	27.79	204
Sum	5832.8	9333.19	17391
Count	463	463	463

## Taxi-out (Mean by Hour)

**Taxi-out Times** 



#### Taxi-out (Mean and Range by Hour)

#### **Taxi-out Times**



## What is Next?

- Introducing quadratic components into the alternative models
- Analyze the effectiveness of taxi time models for a large set of airports
- Test the effect of different scheduling with the same daily total demand
- Investigate the effect of having more (double? Triple?) scheduled flights

# Work in Progress (1)

- Integrated model for departure sequence and gate push-back time
  - Existing literature: Departure sequence with holding point constraint
  - Existing literature: Gate push-back time given departure sequence from SMS





## Multiple Objective Optimization

- Maximizing operational throughput Minimizing late take-off penalty: pushing flight to take off in earlier time periods by penalizing takeoffs in later time periods heavier
- Minimizing taxiing time, including transverse time and taxiing delay
- Minimizing the penalty of deviating from scheduled departure time

# Work in Progress (2)

- Impact of Airport Delay on National System
  - Analyze the delay trend at OEP airports
  - Investigate the change of delay concentration with topology tools
  - Quantify the impact of a single airport or regional airport system to NAS

#### Thank you !

#### Yu Zhang yuzhang@eng.usf.edu