### **ATL Capacity Profiles**



# Overview

- Background and Motivation
- Queueing Models
- Approach
- Experiments
- Results
- On-going Research

#### Deterministic / stochastic model comparisons

Average Delay per Flight (min)



#### Deterministic / stochastic model comparisons

Average Delay per Flight (min)



### Interpretation

- Shift from highly stochastic to fully
- deterministic system reduces delay by 10% plus 1 minute per flight
- Evening schedule to have even inter-arrival times within each 15-minute interval reduces delay by an additional 4% plus 1 minute per flight

#### **Comparison of Delay Profiles (SFO)**

**Total Delays at SFO (min)** 



#### **Comparison of Delay Profiles (ATL)**

Total Delays at ATL (min)



#### **Comparison of Delay Profiles (BOS)**

Total Delays at BOS (min)



S. North

### Conjecture

- Largest differences between stochastic and deterministic cases arise when
  - multiple congested periods exist
  - the system has time to recover between these periods in the deterministic case, but is not able to do so in the stochastic case

### Conclusions

- Highly deterministic system enabled by 4D trajectory precision would reduce delay 10-14% plus 1-2 min per flight (*all else equal*)
- Result holds over a wide range of congestion levels
- Improvement may be greater under certain congestion profiles
- Queueing models are a useful complement to simulation models in examining these matters

# Overview

- Background and Motivation
- Queueing Models
- Approach
- Experiments
- Results
- On-going Research

### Intermediate Levels of Trajectory Precision

Two approaches:

- 1. Extend the Deterministic Queueing Model by Assigning Lateness Errors to Flights
- 2. Think of Queue Length as a mass, and model its diffusion over time

#### **Metered Time Adherence Error Model**

- Each flight is assigned a **Scheduled Time of Arrival**, which it meets with some **imprecision error**
- <u>Inputs</u>: Metered schedule of arrivals; safety separation headways, level of adherence error
- <u>Approach</u>: Model time of arrivals as normal random variables (*with standard deviation representing adherence error*)
- <u>Outputs</u>: Expected delay of all flights; average number of flights in queue; average waiting time per flight, etc.

#### **Metered Time Adherence Error Model**

#### Actual Times of Arrival as Normal Random Variables



# Metered Time Adherence Error Model

- Application:
  - Estimate delays due to imperfect adherence to metered arrival times
  - <u>Inputs</u>: Time spacing between consecutive metered arrivals m; minimum headway h; level of adherence error o
  - <u>Assumption</u>: Flights do not overtake each other (adherence errors are small)
  - <u>Sample Application</u>: Stream of flights for landing, runway as meter point, freeze horizon is 400 nmi

#### **Metered Time Adherence Error Model**



- 1. Compute  $\Delta = (m-h)/\sigma$
- 2. Select corresponding curve
- Multiply values in vertical axis by σ

# Metered Time Adherence Error Model – Next Steps

- Include two types of aircraft: 4DT equipped (high precision) and non-equipped (low precision) aircraft
- Re-sequencing of arrivals:
  - Cases where precision errors are large enough
  - Flights don't arrive at the meter fix in the scheduled order

### **Diffusion Approximation**

- Queue Length can be expressed on a continuum, which is approximately true when very large numbers of customers are involved
- Solve the Kolmogorov Forward Diffusion Equation:

 $f_i(x;t)$  = density of length of queue *i* at time *t* 

