



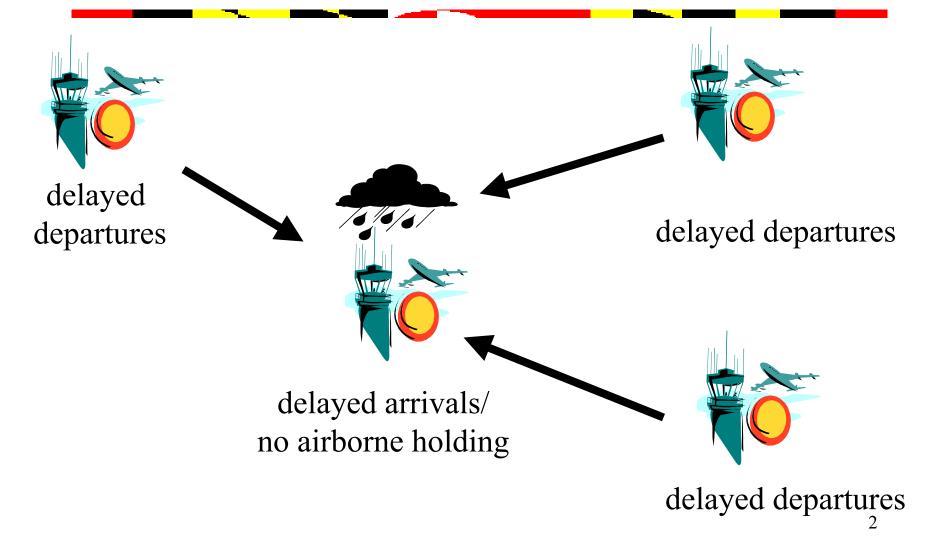
# Fair Allocation Concepts in Air Traffic Management

Thomas Vossen, Michael Ball R.H. Smith School of Business & Institute for Systems Research University of Maryland





Ground Delay Programs







# Collaborative Decision-Making

#### Traditional TFM:

• Flow managers alter routes/schedules of individual flights to achieve system wide performance objectives

### Collaborative Decision-Making (CDM)

• airlines and aircraft operators share information and collaborate in determining resource allocation

#### CDM in GDP context:

- CDM-net, communications network that allows real-time information exchange
- Allocation procedures that increase airline control and encourage airline provision of up-to-date information





### GDPs under CDM

**Resource Allocation Process:** 

- FAA: *initial "fair" slot allocation* [Ration-by-schedule]
- Airlines: *flight-slot assignments/reassignments* [Cancellations and substitutions]
- FAA: *periodic reallocation to maximize slot utilization* [Compression]

Note:

- reduced capacity is partitioned into sequence of arrival slots

- ground delays are derived from delays in arrival time





# Allocating Slots under CDM

*Ration-By-Schedule*:

Step 1: Order flights by their

original scheduled time of arrival

- Step 2: Select the first flight that has not been assigned an arrival slot.
  - assign the selected flight to the earliest unassigned slot
  - repeat step 2.

The resulting allocation is independent of current status of flights and is not affected by status information given by airlines!!



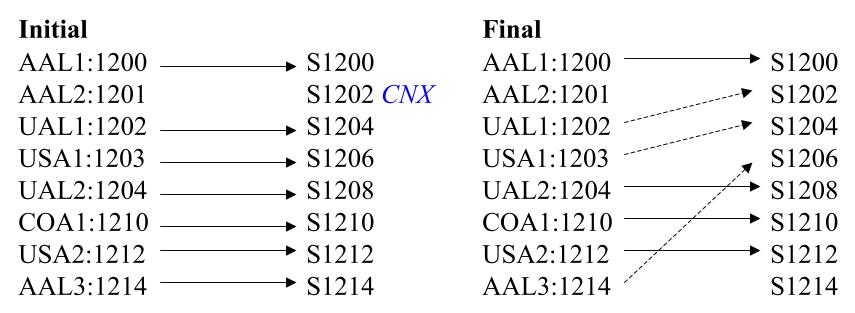


# Slot Reallocation under CDM

#### **Need for Inter-airline slot exchange:**

slots made available through flight cancellations and delays

#### **Compression Algorithm**







### Motivation

### **Fairness Issues:**

- Flight-based vs. airline-based,
  - e.g. RBS:flight-based, Compression: airline-based
- Possible "standards of comparison"
- Impact of program dynamics
  - flight cancellations/delays (compression)
  - flight exemptions





## Related Allocation Problems

Apportionment problems:

• *How to assign house seats to states according to proportion of their populations* 

Balanced just-in-time scheduling problems:

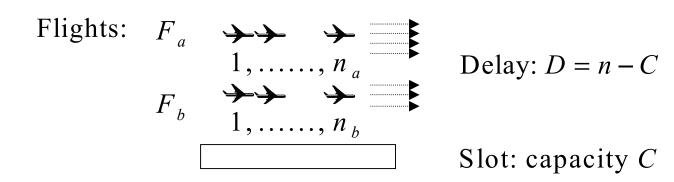
• How to determine production schedules that minimize variation in the production rate of successive units of different product types.





## GDPs as apportionment

"Coarse-grained" one-period GDP:



Interpretation as apportionment:

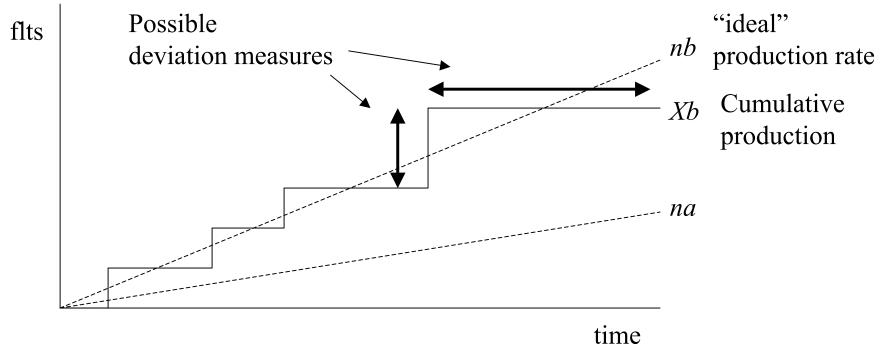
- capacity C = house seats
- airlines = states
- flights = populations





### GDPs as balanced JIT problem

#### "Finer-grained" GDP:

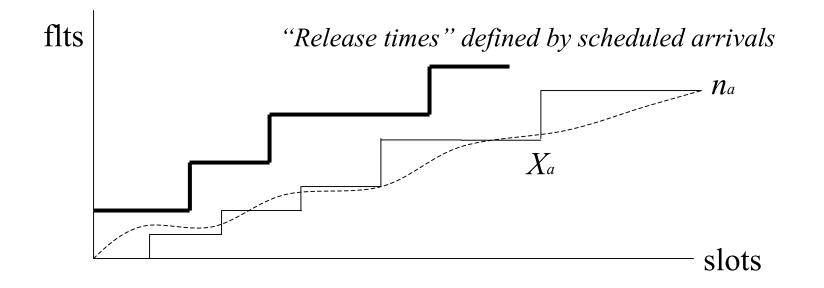


- Airlines = products, flights = product quantities
- Minimize deviation between "ideal" rate and actual production





### **GDP** Situation



Questions:

- What are appropriate "production rates"?
- How to minimize deviations ?
- Managing program dynamics





# Determining fair shares

Sketch:

- Assume slots are *divisible* 
  - leads to probabilistic allocation schemes
- Approach: impose properties that schemes need to satisfy
  - fairness properties
  - structural properties (consistency, sequenceindependence)





# Determining fair shares

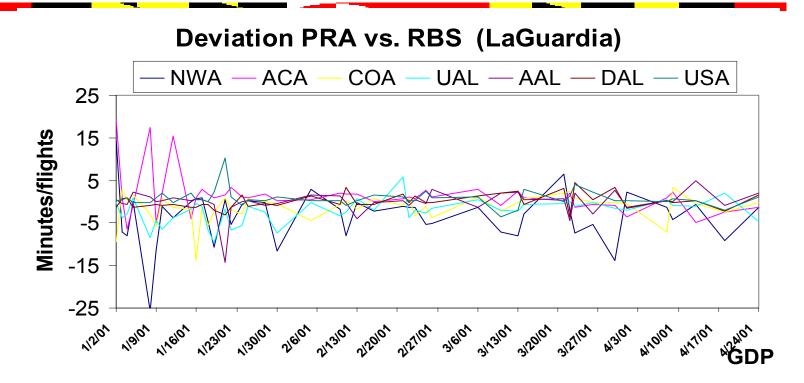
Two possibilities:

- earlier flights have priority over later flights - *e.g. Ration-by-schedule*
- all flights have equal priority
  - leads to "proportional random assignment":
  - At each step, assign next slot to airline *a* with probability proportional to airlines' current flights.





### **Empirical Comparison**



- On the aggregate, both methods give similar shares
- no systematic biases





**Program Dynamics** 

Question:

• If RBS is fine, why bother with minimizing deviation, balancing the schedule ?

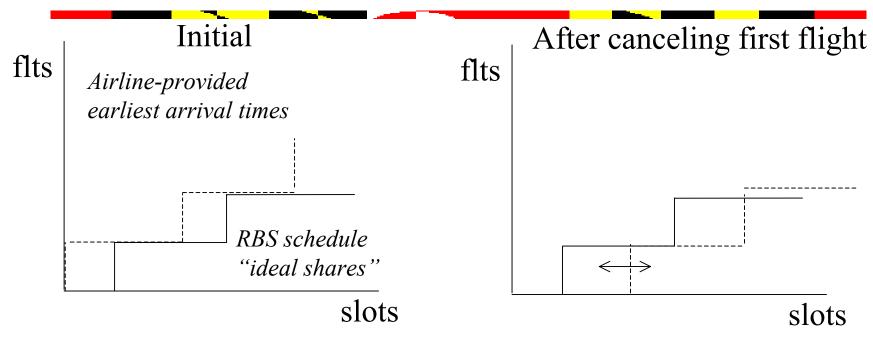
Answer: GDP dynamics

- Flight cancellations, delays (e.g. compression)
- Exemption-handling





# 1.Flight Cancellations/Delays



- Infeasibility/suboptimality require rescheduling
- Use balanced jit paradigm to minimize airline deviations from RBS schedule





# 1.Flight Cancellations/Delays

### Approach:

• Minimize deviation between ideal and actual position for *k*-th flight of airline *a*, for all *a*,*k* 

#### Priority Method:

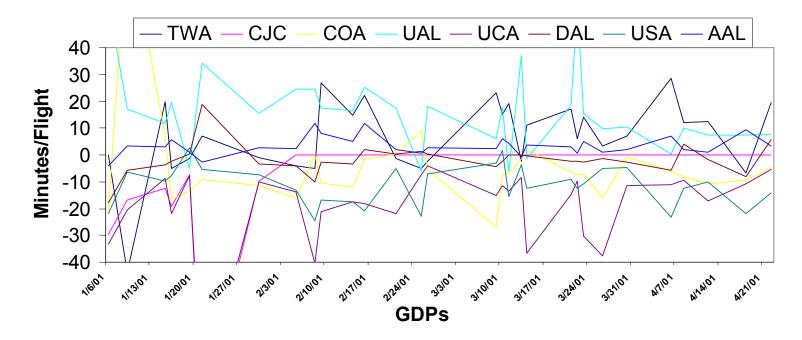
- Input: ordered list of priorities for each airline
- Sequentially assign slots:
  - Assign current slot to airline with highest remaining priority that can use slot (given its earliest arrival times)
- Results similar to compression algorithm





# 2. Flight exemptions

Deviation RBS (standard) vs RBS (+exemptions), Boston



Flight exemptions introduce systematic biases:

• USA (11m/flt), UCA (18m/flt) "lose" under exemptions





# 2. Flight Exemptions

Objective :

- Use deviation model to mitigate exemption bias
  - e.g. "inverse" compression

### Possible approaches:

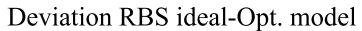
- Optimization model adjusted for constraints posed by exempted flights
- Adjustment of priority method
  - may not minimize overall deviation measure

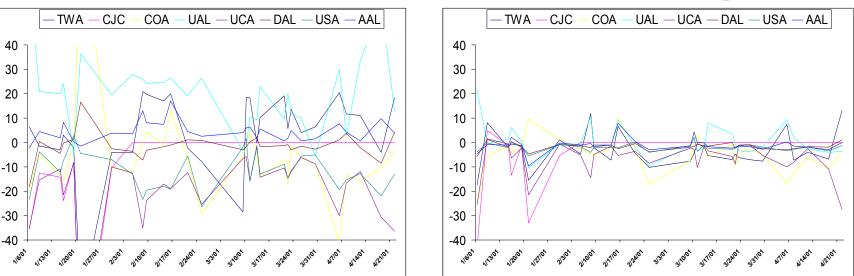




## 2. Flight Exemptions

Deviation RBS ideal-RBS actual





- Minimize deviations using optimization model that incorporates exemptions
- reduces systematic biases, e.g. USA from 11m/flt to 2m/flt, UCA from 18m/flt to 5m/flt

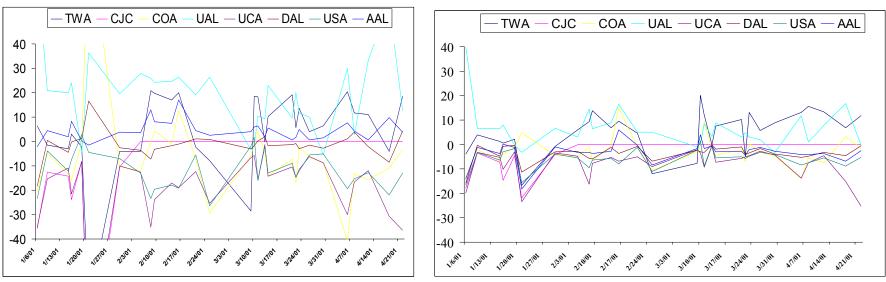




## 2. Flight Exemptions

Deviation RBS ideal-RBS actual

Deviation RBS ideal-priority alg.



- Minimize deviations using adjustment of priority scheme
- lesser, but still significant bias reduction, e.g. USA from 11m/flt to 5m/flt, UCA from 18m/flt to 7m/flt





### Discussion

Approach yields system where:

- airlines are assigned priority *lists* 
  - based on sched. arr. times, constant during GDP
- dynamic changes (capacity, airline data) initiate (re)rationing
  - ration according to *airline* priorities
- priority scheme cannot (completely) be maintained with flight exemptions
  - deviation model shows potential to reduce exemption bias